## Operations and Algebraic Thinking

Write and interpret numerical expressions.

1
Use parentheses, brackets, or braces in numerical expressions, and evaluate expressions with these symbols.

Write simple expressions that record calculations with numbers, and interpret numerical
2 expressions without evaluating them. For example, express the calculation "add 8 and 7, then multiply by 2 " as $2 \times(8+7)$. Recognize that $3 \times(18932+921)$ is three times as large as $18932+921$, without having to calculate the indicated sum or product.

Analyze patterns and relationships.
Generate two numerical patterns using two given rules. Identify apparent relationships between corresponding terms. Form ordered pairs consisting of corresponding terms from the two patterns, and graph the ordered pairs on a coordinate plane. For example, given the rule "Add 3 " and the starting number 0 , and given the rule "Add 6 " and the starting number 0 , generate terms in the resulting sequences, and observe that the terms in one sequence are twice the corresponding terms in the other sequence. Explain informally why this is so.

| Number and Operations in Base Ten |  |  |  |  |  |  |  | 5.NBT |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Understand the place value system. |  | Cycle $1$ | $\begin{gathered} \text { Cycle } \\ 2 \end{gathered}$ | Cycle | Cycle | $\begin{gathered} \text { Cycle } \\ 5 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 6 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 7 \end{gathered}$ | Cycle 8 |
| 1 | Recognize that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and $1 / 10$ of what it represents in the place to its left. |  |  |  |  |  |  |  |  |
| 2 | Explain patterns in the number of zeros of the product when multiplying a number by powers of 10, and explain patterns in the placement of the decimal point when a decimal is multiplied or divided by a power of 10 . Use whole-number exponents to denote powers of 10. |  | $\bigcirc$ |  | $\bigcirc$ |  | $\bigcirc$ |  | $\bigcirc$ |
| 3 | Read, write, and compare decimals to thousandths. |  | $\bigcirc$ |  | $\bigcirc$ |  |  |  |  |
| Perform operations with multi-digit whole numbers and with decimals to hundredths. |  | Cycle | $\begin{gathered} \text { Cycle } \\ 2 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 3 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 4 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 5 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 6 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 7 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 8 \end{gathered}$ |
| 7 | Add, subtract, multiply, and divide decimals to hundredths, using concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; relate the strategy to a written method and explain the reasoning used. | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |


| Number and Operations - Fractions |  |  |  |  |  |  |  | 5.NF |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Use equivalent fractions as a strategy to add and subtract fractions. |  | Cycle $1$ | Cycle | Cycle | Cycle | $\begin{gathered} \text { Cycle } \\ 5 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 6 \end{gathered}$ | Cycle | Cycle 8 |
| 1 | Add and subtract fractions with unlike denominators (including mixed numbers) by replacing given fractions with equivalent fractions in such a way as to produce an equivalent sum or difference of fractions with like denominators. For example, $2 / 3+5 / 4=8 / 12+15 / 12=23 / 12$. (In general, $a / b+c / d=(a d+b c) / b d$.) | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - | - | - | $\bigcirc$ | - |
| Use equivalent fractions as a strategy to add and subtract fractions. |  | Cycle | Cycle | $\begin{gathered} \text { Cycle } \\ 3 \end{gathered}$ | Cycle | $\begin{gathered} \hline \text { Cycle } \\ 5 \end{gathered}$ | $\begin{array}{\|c\|} \hline \text { Cycle } \\ \hline \end{array}$ | $\begin{gathered} \text { Cycle } \\ 7 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 8 \end{gathered}$ |
| 3 | Interpret a fraction as division of the numerator by the denominator $(a / b=a \div b)$. Solve word problems involving division of whole numbers leading to answers in the form of fractions or mixed numbers, e.g., by using visual fraction models or equations to represent the problem. For example, interpret $3 / 4$ as the result of dividing 3 by 4, noting that $3 / 4$ multiplied by 4 equals 3 , and that when 3 wholes are shared equally among 4 people each person has a share of size $3 / 4$. If 9 people want to share a 50 -pound sack of rice equally by weight, how many pounds of rice should each person get? Between what two whole numbers does your answer lie? | - |  | $\bigcirc$ |  |  |  |  |  |
| 4 | Apply and extend previous understandings of multiplication to multiply a fraction or whole number by a fraction. | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| 7 | Apply and extend previous understandings of division to divide unit fractions by whole numbers and whole numbers by unit fractions. (Students able to multiply fractions in general can develop strategies to divide fractions in general, by reasoning about the relationship between multiplication and division. But division of a fraction by a fraction is not a requirement at this grade.) | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - |

## The Number System

|  | m | 5.NS |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Gain familiarity with concepts of positive and negative integers. |  | $\begin{gathered} \text { Cycle } \\ 1 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 2 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 3 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 4 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 5 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 6 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 7 \end{gathered}$ | Cycle 8 |
| MA | Use positive and negative integers to describe quantities such as temperature above/ below zero, elevation above/below sea level, or credit/debit. |  | - |  | - |  | $\bigcirc$ |  | - |



| easurement and Data 5 5.MD |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Convert like measurement units within a given measurement system. |  | Cycle | $\begin{gathered} \text { Cycle } \\ 2 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 3 \end{gathered}$ | Cycle | $\begin{gathered} \text { Cycle } \\ 5 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 6 \end{gathered}$ | Cycle | Cycle 8 |
| 1 | Convert among different-sized standard measurement units within a given measurement system (e.g., convert 5 cm to 0.05 m ), and use these conversions in solving multi-step, real-world problems. | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - |
| Represent and interpret data. |  | $\begin{gathered} \hline \text { Cycle } \\ 1 \\ \hline \end{gathered}$ | $\begin{array}{\|c} \hline \text { Cycle } \\ 2 \end{array}$ | Cycle | Cycle | Cycle | Cycle | Cycle | Cycle 8 |
| 2 | Make a line plot to display a data set of measurements in fractions of a unit (1/2, 1/4, $1 / 8)$. Use operations on fractions for this grade to solve problems involving information presented in line plots. For example, given different measurements of liquid in identical beakers, find the amount of liquid each beaker would contain if the total amount in all the beakers were redistributed equally. |  | $\bigcirc$ |  | $\bigcirc$ |  | $\bigcirc$ |  | - |
| Geometric measurement: understand concepts of volume and relate volume to multiplication and to addition. |  | Cycle | $\begin{gathered} \text { Cycle } \\ 2 \end{gathered}$ | Cycle w3 | $\begin{gathered} \text { Cycle } \\ 4 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 5 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 6 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 7 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 8 \end{gathered}$ |
| 3 | Recognize volume as an attribute of solid figures and understand concepts of volume measurement. |  | $\bigcirc$ |  | - |  | - |  | - |
| 4 | Measure volumes by counting unit cubes, using cubic cm , cubic in, cubic ft , and improvised units. |  | $\bigcirc$ |  | - |  | - |  | $\bigcirc$ |
| 5 | Relate volume to the operations of multiplication and addition and solve real-world and mathematical problems involving volume. |  | $\bigcirc$ |  | $\bigcirc$ |  | $\bigcirc$ |  | $\bigcirc$ |



| Ratios and Proportional Relationships |  |  |  |  |  |  |  | 6.RP |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Understand ratio concepts and use ratio reasoning to solve problems |  | $\begin{gathered} \text { Cycle } \\ 1 \\ \hline \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 2 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 3 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 4 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 5 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 6 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 7 \end{gathered}$ | $\begin{gathered} \hline \text { Cycle } \\ 8 \end{gathered}$ |
| 1 | Understand the concept of a ratio and use ratio language to describe a ratio relationship between two quantities. For example, "The ratio of wings to beaks in the bird house at the zoo was $2: 1$, because for every 2 wings there was 1 beak." "For every vote candidate A received, candidate C received nearly three votes." |  |  |  |  | - |  | $\bigcirc$ |  |
| 2 | Understand the concept of a unit rate $a / b$ associated with a ratio $a: b$ with $b^{1} 0$, and use rate language in the context of a ratio relationship. For example, "This recipe has a ratio of 3 cups of flour to 4 cups of sugar, so there is $3 / 4$ cup of flour for each cup of sugar." "We paid $\$ 75$ for 15 hamburgers, which is a rate of $\$ 5$ per hamburger." [1] |  |  |  |  |  | - |  | - |
| 3 | Use ratio and rate reasoning to solve real-world and mathematical problems, e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or equations. |  |  |  |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |


| Geometry |  |  |  |  |  |  |  | 6.G |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Solve real-world and mathematical problems involving area, surface area, and volume. |  | Cycle | Cycle | Cycle | $\begin{gathered} \text { Cycle } \\ 4 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 5 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 6 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 7 \end{gathered}$ | Cycle 8 |
| 1 | Find the area of right triangles, other triangles, special quadrilaterals, and polygons by composing into rectangles or decomposing into triangles and other shapes; apply these techniques in the context of solving real-world and mathematical problems. | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - |
| 2 | Find the volume of a right rectangular prism with fractional edge lengths by packing it with unit cubes of the appropriate unit fraction edge lengths, and show that the volume is the same as would be found by multiplying the edge lengths of the prism. Apply the formulas $\mathrm{V}=\mathrm{I} \mathrm{wh}$ and $\mathrm{V}=\mathrm{b} \mathrm{h}$ to find volumes of right rectangular prisms with fractional edge lengths in the context of solving real-world and mathematical problems. |  | $\bigcirc$ |  | - |  | $\bigcirc$ |  | - |
| 3 | Draw polygons in the coordinate plane given coordinates for the vertices; use coordinates to find the length of a side joining points with the same first coordinate or the same second coordinate. Apply these techniques in the context of solving real-world and mathematical problems. | $\bigcirc$ |  | - |  |  | $\bigcirc$ |  | $\bigcirc$ |
| 4 | Represent three-dimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures. Apply |  |  |  |  | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |

## Expressions and Equations

6.EE

| Apply and extend previous understandings of arithmetic to algebraic expressions. |  | ${ }_{\text {Cycle }}$ | Cycle | ${ }_{\text {cycle }}$ | ${ }_{4}^{\text {Cycle }}$ | ${ }_{\text {cycle }}$ | ${ }_{\text {Cycle }}$ | ${ }_{\text {Cycle }}$ | Cycle |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Write and evaluate numerical expressions involving whole-number exponents. | - | - | - | $\bigcirc$ |  | - |  | $\bigcirc$ |
| 2 | Write, read, and evaluate expressions in which letters stand for numbers. | - | - | - | $\bigcirc$ | - |  | $\bigcirc$ |  |
| 3 | Apply the properties of operations to generate equivalent expressions. For example, apply the distributive property to the expression $3(2+x)$ to produce the equivalent expression $6+3 x$; apply the distributive property to the expression $24 \mathrm{x}+18 \mathrm{y}$ to produce the equivalent expression 6 ( $4 \mathrm{x}+$ $3 y$ ); apply properties of operations to $\mathrm{y}+\mathrm{y}+\mathrm{y}$ to produce the equivalent expression 3 y . | - | - |  | - | - | - | - | $\bigcirc$ |
| 4 | Identify when two expressions are equivalent (i.e., when the two expressions name the same number regardless of which value is substituted into them). For example, the expressions $y+y$ +y and 3 y are equivalent because they name the same number regardless of which number y stands for. | - |  |  |  | - |  | $\bigcirc$ |  |
| Reason about and solve one-variable equations and inequalities. |  | Cycle | cycle | Cycle | Cycle | Cycle | $\begin{array}{\|c} \text { cycle } \end{array}$ | $\underset{7}{\text { cycle }}$ | ${ }_{8}^{\text {cycle }}$ |
| 5 | Understand solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? Use substitution to determine whether a given number in a specified set makes an equation or inequality true. |  | - |  |  | $\bigcirc$ |  | $\bigcirc$ |  |
| 6 | Use variables to represent numbers and write expressions when solving a real-world or mathematical problem; understand that a variable can represent an unknown number, or, depending on the purpose at hand, any number in a specified set. |  |  |  |  |  | $\bigcirc$ |  | $\bigcirc$ |
| 7 | Solve real-world and mathematical problems by writing and solving equations of the form $\mathrm{x}+\mathrm{p}=\mathrm{q}$ and $\mathrm{px}=\mathrm{q}$ for cases in which $\mathrm{p}, \mathrm{q}$ and x are all nonnegative rational numbers. |  | - |  |  | - |  | - |  |
| 8 | Write an inequality of the form $\mathrm{x}>\mathrm{c}$ or $\mathrm{x}<\mathrm{c}$ to represent a constraint or condition in a real-world or mathematical problem. Recognize that inequalities of the form $\mathrm{x}>\mathrm{c}$ or $\mathrm{x}<\mathrm{c}$ have infinitely many solutions; represent solutions of such inequalities on number line diagrams. |  |  |  |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - |
| Represent and analyze quantitative relationships between dependent and independent variables. |  | cycle | $\underset{2}{\text { Cycle }}$ | $\begin{gathered} \text { cycle } \end{gathered}$ | ${ }_{4}$ Cycle | $\begin{gathered} \text { Cycle } \\ 5 \end{gathered}$ | $\begin{gathered} \text { cycle } \end{gathered}$ | ${ }_{7}$ | ${ }_{8}^{\text {Cycle }}$ |
| 9 | Use variables to represent two quantities in a real-world problem that change in relationship to one another; write an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. Analyze the relationship between the dependent and independent variables using graphs and tables, and relate these to the equation. For example, in a problem involving motion at constant speed, list and graph ordered pairs of distances and times, and write the equation $d=65 t$ to represent the relationship between distance and time. |  | - | $\bigcirc$ | - |  |  |  |  |

## Statistics and Probability

| Develop understanding of statistical variability. |  | $\begin{gathered} \text { Cycle } \\ 1 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 2 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 3 \end{gathered}$ | $\underset{4}{\mathrm{Cycle}}$ | $\underset{5}{\text { Cycle }}$ | $\begin{gathered} \text { Cycle } \\ 6 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 7 \end{gathered}$ | $\begin{gathered} \text { Cycle } \\ 8 \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Recognize a statistical question as one that anticipates variability in the data related to the question and accounts for it in the answers. For example, "How old am I?" is not a statistical question, but "How old are the students in my school?" is a statistical question because one anticipates variability in students' ages. |  | $\bigcirc$ |  | - |  | - |  | $\bigcirc$ |
| 2 | Understand that a set of data collected to answer a statistical question has a distribution which can be described by its center, spread, and overall shape. |  |  |  |  | - |  | $\bigcirc$ | $\bigcirc$ |
| 3 | Recognize that a measure of center for a numerical data set summarizes all of its values with a single number, while a measure of variation describes how its values vary with a single number. |  |  |  |  | $\bigcirc$ |  | - | - |
| Summarize and describe distributions. |  | Cycle | Cycle | Cycle | Cycle | $\begin{gathered} \text { Cycle } \end{gathered}$ | $\underset{6}{\text { Cycle }}$ | Cycle | Cycle 8 |
| 4 | Display numerical data in plots on a number line, including dot plots, histograms, and box plots. | $\bigcirc$ |  | - | - | - | - | $\bigcirc$ | - |
| 5 | Summarize numerical data sets in relation to their context, such as by: |  |  |  |  |  |  |  |  |
|  a. Reporting the number of observations. <br>  b. Describing the nature of the attribute under investigation, including how it was mea- <br> sured and its units of measurement. <br>  c. Giving quantitative measures of center (median and/or mean) and variability (inter- <br> quartile range and/or mean absolute deviation), as well as describing any overall pattern <br> and any striking deviations from the overall pattern with reference to the context in which <br> the data were gathered. |  |  | - |  | - |  | - |  | $\bigcirc$ |
|  |  |  |  |  | $\bigcirc$ |  | $\bigcirc$ |  |  |
|  |  |  |  |  |  | $\bigcirc$ |  | $\bigcirc$ | $\bigcirc$ |

